

Percentages

Converting between fractions, decimals and percentages.



1. Without a calculator:

$$0.35 = \frac{35}{100} = \frac{7}{20} = 35\%$$

$$\frac{2}{5} = \frac{4}{10} = \frac{40}{100} = 0.4 = 40\%$$

$$8\% = \frac{8}{100} = \frac{2}{25} = 0.08$$

Examples:

Without a calculator find the fraction, decimal and percentage equivalents.

$$1) \frac{4}{5} = \frac{8}{10} = \frac{80}{100} = 80\% = 0.8$$

$$2) 75\% = \frac{75}{100} = 0.75 = \frac{3}{4}$$

$$3) 0.7 = \frac{7}{10} = \frac{70}{100} = 70\%$$

2. With a calculator:

$$\frac{3}{8} = 3 \div 8 = 0.375 = 37.5\%$$

↖
×100

$$a) \frac{2}{7} = 0.2857 = 28.57\%$$

$$b) \frac{9}{11} = 0.8181 = 81.81\%$$

$$c) \frac{16}{49} = 0.3265 = 32.65\%$$

Write these percentages as fractions:

$$59\% = \frac{59}{100}$$

$$91.7\% = \frac{917}{1000}$$

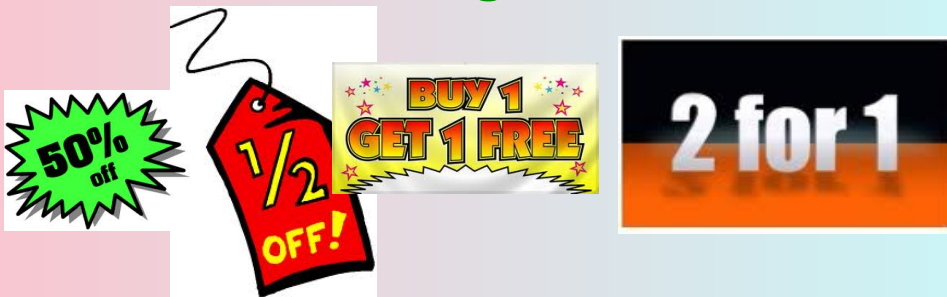
$$8.3\% = \frac{83}{1000}$$

$$60\% = \frac{60}{100} = \frac{3}{5}$$

$$7\% = \frac{7}{100}$$

$$20\% = \frac{20}{100} = \frac{1}{5}$$

Match the bargains



Finding a percentage of an amount.

without a calculator!

75% = 30 30% = 12 10% = 4
99% = 39.6

1% = 0.4 **40**

15% = 6

25% = 10 4% = 1.6 2.5% = 1
0.4 0.4 0.2
1% 1% 1/2

75% = 45 30% = 18 10% = 6

99% = 59.4

1% = 0.6 **60**

50% = 30
25% = 15

15% = 9

17 1/2% = 10.5

25% = 15

4% = 2.4

2.5% = 1.5

£ 8.20

Here's a recipe for muesli squares.

MUESLI SQUARES

Makes 15

75 g butter
30 ml golden syrup
45 g soft brown sugar
165 g muesli
45 g glacé cherries
105 g plain chocolate, melted

465

sugar = 9.7%

What percentage of the bake is:

a) butter

$$\frac{75}{465} = 0.1612... = 16.1\%$$

b) golden syrup

$$\frac{30}{465} = 0.0645 = 6.5\%$$

c) sugar

$$\frac{45}{465} = 0.0967 = 9.7\%$$

d) muesli

$$\frac{165}{465} = 0.354 = 35.5\%$$

e) cherries

$$\frac{45}{465} = 9.7\%$$

Changing Fractions to Percentages

Janet and John both came home with test results.

Janet had $\frac{8}{10}$ for Maths and John had $\frac{18}{23}$ for English.

Their parents gave John a bag of sweets for getting 18 but made ~~Karen~~ Janet do extra homework for getting only 8.

How fair is that?



$$\frac{8}{10} = 80\%$$

$$78.3\% = \frac{18}{23}$$



Janet had a score of 80%, so it was unfair

One number as a percentage of another

page 109 C1-C5

Homework for Friday

Page 115 Test yourself

Finding a percentage of an amount using a calculator.

Find 17% of 65 $\frac{17}{100} \times 65$
 $= 0.17 \times 65$
 $= 11.05$
 Find 43% of 16 $= 6.88$

Page 111 E1-6

Increase/decrease by a percentage

Increase £62 by 10%

<p>method 1</p> <p>Find 10% of 62 add it on to 62 10% of 62 = 6.2</p> $\begin{array}{r} 62.0 \\ + 6.2 \\ \hline 68.2 \end{array}$	<p>method 2</p> $\frac{110}{100} \times 62$ $= 1.10 \times 62$ $= 68.2$
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Increase £62 by 14%

<p>method 1</p> <p>Find 14% of 62 $0.14 \times 62 = 8.68$ $62 + 8.68 = 70.68$</p>	<p>method 2</p> $\frac{114}{100} \times 62$ $= 70.68$
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~~Decrease~~ £62 by 10%

<p>method 1</p> <p>10% of 62 = 6.20 $62 - 6.20 = 55.80$ £55.80</p>	<p>method 2</p> $\frac{90}{100} \times 62$ $= 55.80$
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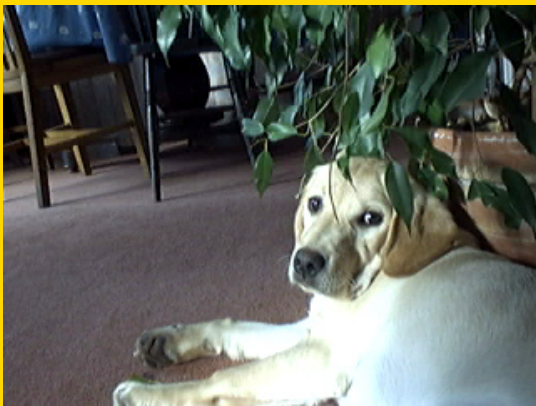
Decrease £62 by 17%

<p>method 1</p> <p>$\frac{17}{100} \times 62 = 10.54$ $62 - 10.54 = 51.46$</p>	<p>method 2</p> <p>$\frac{83}{100} \times 62 = 51.46$</p>
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B1, B3, B5
NO
CALCC

page 383 odds only,
page 384/385 odds only

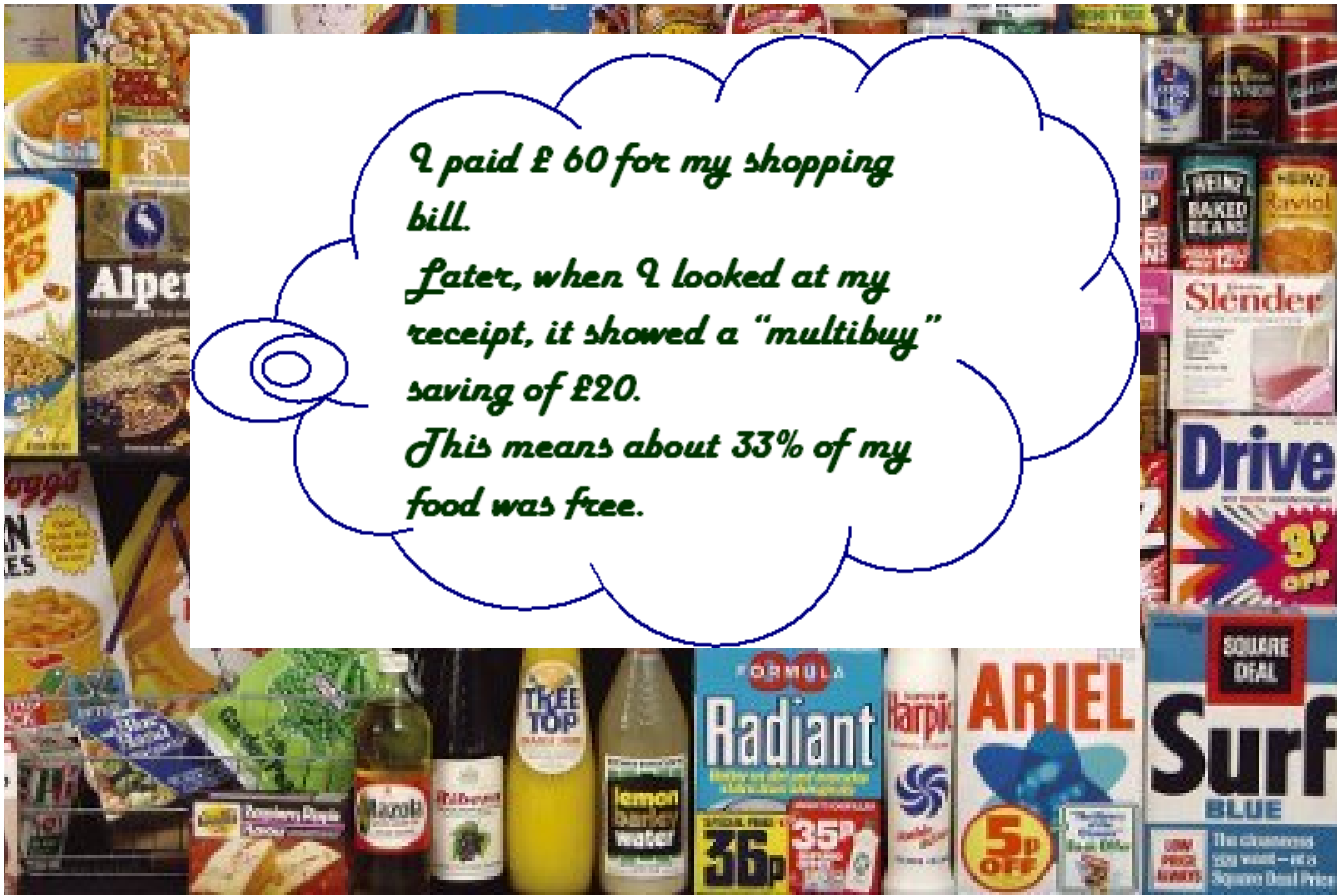
Finding a percentage increase.



In the past 5 years Mabel's weight has increased. She used to weigh 25kg. Now she weighs 30kg. What is the percentage increase?

$$\frac{5}{25} \times 100 = 20\%$$

By what percentage is taller than ?



I paid £ 60 for my shopping bill.

Later, when I looked at my receipt, it showed a "multibuy" saving of £20.

This means about 33% of my food was free.

$$\% \text{ age increase} = \frac{\text{actual increase}}{\text{original}} \times 100$$

$$E1) \frac{20}{250} \times 100 = 8\%$$

$$E3) \frac{120}{400} \times 100 = 30\%$$

Finding a percentage decrease.



Was £5.00

now £3.50

What is the percentage saving?



Suppose a miracle happened and Mabel lost that extra 5kg and returned to her slim 25kg. What would be the percentage decrease in her weight?

$$\text{Percentage decrease} = \frac{\text{Actual decrease}}{\text{original}} \times 100$$

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page 388 odds only

p388

Time Sales



I got a great bargain in the sales. This bag was £15.00 last week. Today it was reduced to £5.00.

$$\frac{10}{15} = 66.6\%$$

$$\frac{20}{50} = 40\%$$

Well, what do you think of this...I spent £30.00 on these trousers and they were priced at £50.00. That's an even better bargain.

Successive percentage changes

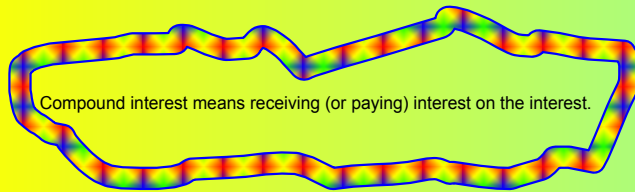
I invest £100 in a bank for 3 years at a rate of 6% interest.
After 3 years I have £118.

True or false?

Explain your answer.



After 1 year: £106
 2nd yr: $106\% \times 106 = 112.36$
 3rd yr: $\frac{106}{100} \times 112.36 = \pounds 119.10$



Compound interest means receiving (or paying) interest on the interest.

Questions C1 and C2.

Suppose you were to invest £100 at 5% per annum find out how much you would get after 2,3,4..years and then 20 years.

Year	Balance
1	105% of 100 = 105
2	105% of 105 = 110.25
3	105% of 110.25 = 115.76
4	
	£265.00

20

Questions C3-C5

Save

I calculated my interest on savings to be

$$150 \times 1.06 \times 1.06 \times 1.06$$

Buying or borrowing?



You want to buy a car.

It costs £4000.

You can buy now and borrow at 20% per year,

or,

you can save earning 6% per year.

You have £150 to put aside per month for the car.

Work out how long you will spend buying the car.

year	saved	+interest
1	£1800 : 12×150	$\frac{106}{100} \times 1800 = 1908$
2	$1908 + 1800$ $= 3708$	$\frac{106}{100} \times 3708 = 3930.4$

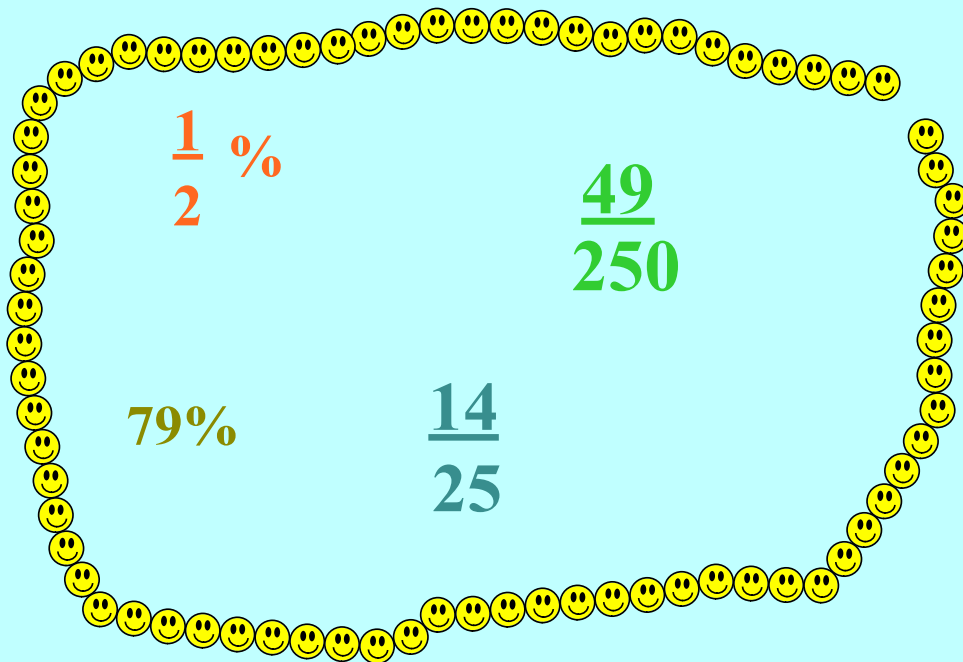
I will need to save for 2 years and 1 month

	Borrow	plus interest	payback	Balance
1	4000	4800	- 1800	3000
2	3000	3600	- 1800	1800
3	1800	2160	- 1800	360
4	360	432		
		3 years +	3 months	
				Total pd back 5832

If you were Aunt Ethel's niece/nephew what would you choose?
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Without a calculator convert each of these to a decimal:





Food has gone up in price recently.
A family shop costs about £100.
If food prices have gone up by about 15% in the last year, how much would you have paid for a shop this time last year.

Attachments

PERCEN~1.PPT

percentages in pieces.ppt